#### **Pittsburg State University**

# Pittsburg State University Digital Commons

Open Educational Resources - Math

Open Educational Resources by Subject Area

8-2017

# Constructing a Square an Ancient Indian Way Activity

Cynthia J. Huffman Ph.D. *Pittsburg State University*, cjhuffman@pittstate.edu

Follow this and additional works at: https://digitalcommons.pittstate.edu/oer-math

Part of the Geometry and Topology Commons, and the Other Mathematics Commons

#### **Recommended Citation**

Huffman, Cynthia J. Ph.D., "Constructing a Square an Ancient Indian Way Activity" (2017). *Open Educational Resources - Math.* 2. https://digitalcommons.pittstate.edu/oer-math/2

This Book is brought to you for free and open access by the Open Educational Resources by Subject Area at Pittsburg State University Digital Commons. It has been accepted for inclusion in Open Educational Resources - Math by an authorized administrator of Pittsburg State University Digital Commons. For more information, please contact digitalcommons@pittstate.edu.

# **Constructing a Square an Ancient Indian Way Activity**

#### **Overview**

In this activity, the students will model constructing a square with a method similar to one used by people in ancient India to build a fire altar. The activity works best with the students working in pairs.

#### Materials for each pair of students

- 3 thumbtacks or push pins
- Square or rectangular piece of corrugated cardboard, e.g. the top of a pizza box, or a flat piece of styrofoam
- Piece of string length should be double the length of the desired side of the square plus some extra for making loops on each end (2 to 4 inches for each loop, depending on the fine motor skills of the students)
- Straightedge
- Marker or pen

#### Instructions

- 1. Tie a loop at each end of the string. (Instructions for tying a perfection loop knot can be found at <a href="http://www.netknots.com/fishing\_knots/perfection-loop/">http://www.netknots.com/fishing\_knots/perfection-loop/</a>.)
- 2. Fold the string in half, and using the marker, mark the midpoint *M* of the string. (The constructed square will have side length equal to the length of the folded string.)



3. Using the straightedge, trace a line segment  $\overline{AM}$  with length the same as half of the string. This segment  $\overline{AM}$  will be the East-West line of the square.



- 4. Fold one-half of the string in half, and using the marker, mark the midpoint of that half of the string, *C*. This point *C* will be used to construct the corners of the square.
- 5. With the same half of the string, fold it in half again and mark the point *N* that is midway between *M* and *C*, i.e. 1/4 of the way past the midpoint of the entire string. In the *Baudhāyana-śulba-sūtra*, this point *N* was called the *nyancana* (pronounced nyan-cha-na).



6. With a pushpin through each loop at the ends of the string, place the pins on the ends of the East-West line segment,  $\overline{AM}$ .



7. Holding the string at the ¼ *nyancana* point *N*, pull the string upwards until it is taut. Use a pushpin to hold the string taut at *N*. Mark on the background the location of the point *C*.



8. Repeat step 7, by pulling the string downwards.



9. Change places with the ends of the string on the East-West line segment,  $\overline{AM}$ . Repeat steps 7 and 8 to construct the other two corners of the square.



10. Draw the square by using the straightedge to connect the four corner points.



11. If desired, use the cord to find the midpoints of the top and bottom of the square to create a North-South line.



### Follow-up Activity

Have the students prove that the result is actually a square, first by proving it is a rhombus (with each side having the length of half the string) and then proving that each interior angle is a right angle. (Hint: use the converse of the Pythagorean Theorem since the triangle formed in Steps 6 and 7 is a 3-4-5 triangle. To see that the triangle *AMN* is a right triangle, start be letting the length of  $\overline{AM}$  be a. Then the string has length 2a and the two sides of the triangle it forms in Step 7 have lengths  $\frac{5}{4}a$  and  $\frac{3}{4}a$ , respectively.)

### **Original Text**

This activity follows closely Paragraph 1.5 of the *Baudhāyana-śulba-sūtra*, in the translation from Sen and Bag (Sen, S.N., and A.K. Bag. The Śulbasūtras. Indian National Science Academy, 1983).

Now another (method). Ties are made at both ends of a cord twice the measure and a mark I given at the middle. This (halving of the cord) is for the east-west line (that is, the side of the required square). In the other half (cord) at a point shorter by one-fourth, a mark is given; this is the nyancana (mark). (Then) a mark is given at the middle (of the same half cord) for purposes of (fixing) the corners (of the square). With the two ties fastened to the two ends of the east-west line (prythyā), the cord is to be stretched towards the south by the nyancana (mark); the middle mark (of the half cord) determines the western and eastern corners (of the square).

### <u>Notes</u>

- The string should not be stretchy.
- Loops on the ends of the string should be fixed so they won't slide.
- When making circles, the pin should be held steady but not flush against the cardboard so that the loops can move freely about the shank of the pin.
- Watch out for the sharp ends of the pins poking through the cardboard or styrofoam.
- <u>Common Core Standard G.CO.12</u> recommends making formal geometric constructions with a variety of tools and methods.